

Fall 2013

4.6 - Other Trig Functions

Define

$$\tan(x) = \frac{\sin(x)}{\cos(x)}$$

$$\csc(x) = \frac{1}{\sin(x)}$$

$$\sec(x) = \frac{1}{\cos(x)}$$

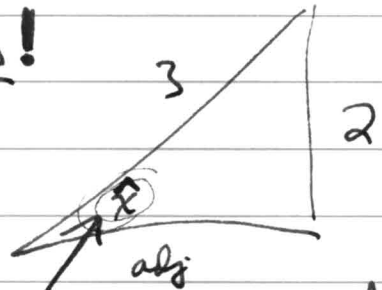
$$\cot(x) = \frac{1}{\tan(x)}$$

4.6 - Other Trig Functions

Suppose $\sin(x) = -\frac{2}{3}$
 and $\frac{3\pi}{2} < x < 2\pi$

Find all 6 trig x 's

Draw a Δ !



$$\text{adj}^2 + 2^2 = 3^2$$

$$\text{adj}^2 = 9 - 4 = 5$$

$$\text{adj} = \sqrt{5}$$

10

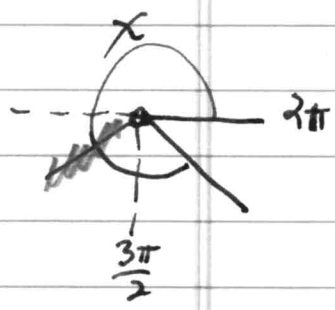
Reference x for x

Evaluate Ref x

Compute value at x

$$\sin \hat{x} = \frac{\text{opp}}{\text{hyp}} = \frac{2}{3}$$

y -coord is negative
 $\Rightarrow \sin(x) = -\frac{2}{3}$



$$\cos \hat{x} = \frac{\text{adj}}{\text{hyp}} = \frac{\sqrt{5}}{3}$$

x -coord is pos
 $\Rightarrow \cos(x) = \frac{\sqrt{5}}{3}$

$$\tan \hat{x} = \frac{\text{opp}}{\text{adj}} = \frac{2}{\sqrt{5}}$$

$\frac{\text{neg}}{\text{pos}} = \text{neg} \Rightarrow \tan(x) = -\frac{2}{\sqrt{5}}$

$$\csc(\hat{x}) = \frac{1}{\sin \hat{x}} = \frac{3}{2}$$

$\frac{1}{\text{neg}} = \text{neg} \Rightarrow \csc(x) = -\frac{3}{2}$

$$\sec(\hat{x}) = \frac{1}{\cos \hat{x}} = \frac{3}{\sqrt{5}}$$

$\frac{1}{\text{pos}} = \text{pos} \Rightarrow \sec(x) = \frac{3}{\sqrt{5}}$

$$\cot(\hat{x}) = \frac{1}{\tan \hat{x}} = \frac{\sqrt{5}}{2}$$

$\frac{1}{\text{neg}} = \text{neg} \Rightarrow \cot(x) = -\frac{\sqrt{5}}{2}$

$$y = \tan(x) = \frac{\sin(x)}{\cos(x)}$$

is undefined whenever $\cos(x) = 0$



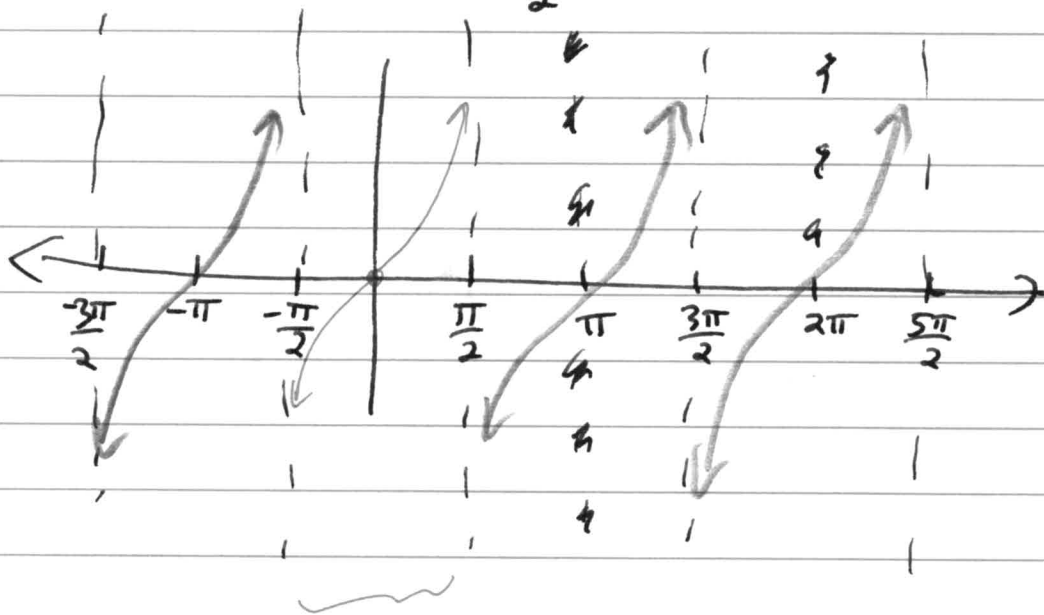
so $\tan(x)$ is undefined at $x = \frac{\pi}{2} + n \cdot \pi$

where n is any integer

10

this gives us vertical asymptotes at each

$$\frac{\pi}{2} + n\pi$$



Draw then explain

$$\frac{\sin(x)}{\cos(x)} \rightarrow \frac{1}{0 \text{ as pos } \#} \Rightarrow \tan(x) \rightarrow +\infty$$

$$\frac{\sin(x)}{\cos(x)} \rightarrow \frac{-1}{0 \text{ as pos } \#} \Rightarrow \tan(x) \rightarrow -\infty$$

then say this repeats everywhere.

Notice: $\tan(x)$ has period π .

Graph $f(x) = \tan(2x)$

$f(x) = \tan(2x)$ has period is $\frac{\pi}{2}$

check

~~tan~~

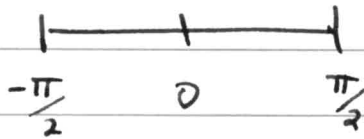
$$f\left(x + \frac{\pi}{2}\right) = \tan\left(2\left(x + \frac{\pi}{2}\right)\right)$$

$$= \tan(2x + \pi)$$

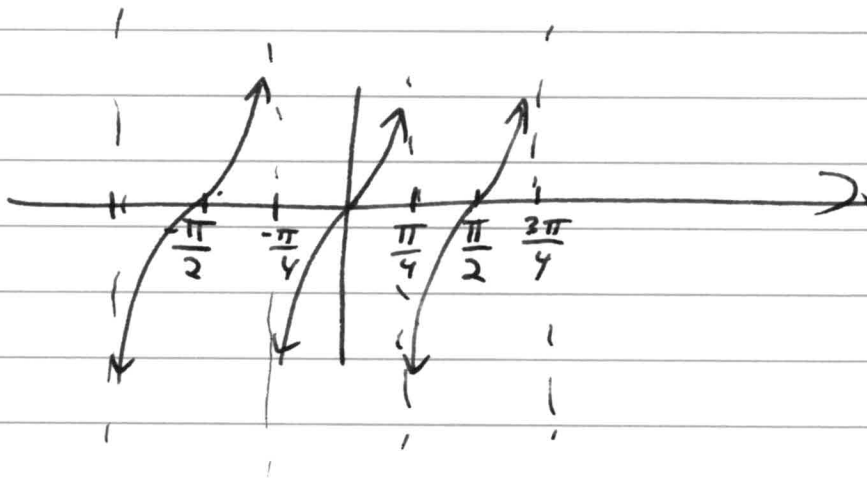
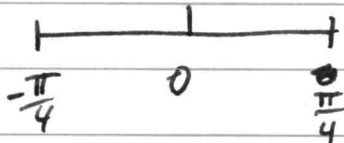
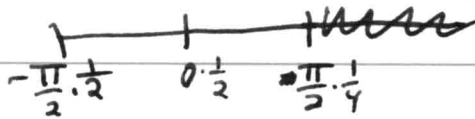
$$= \tan(2x)$$

$$f\left(x + \frac{\pi}{2}\right) = f(x)$$

idea

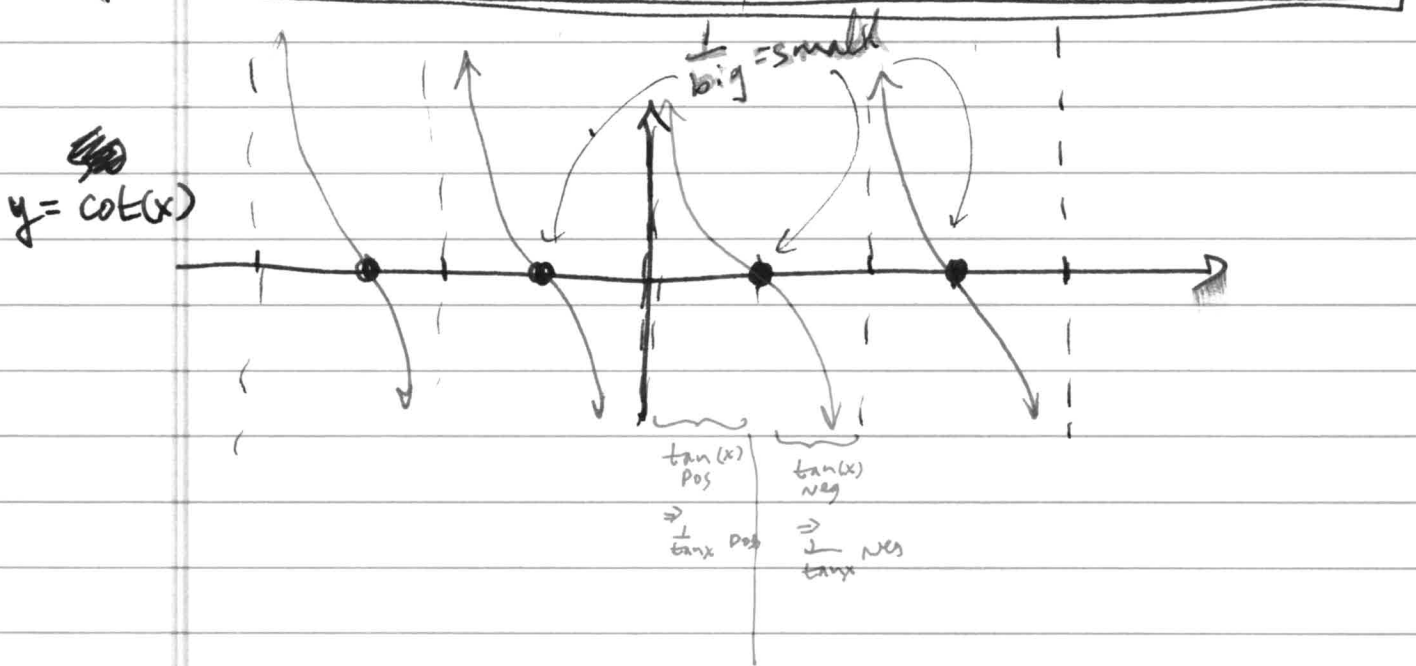
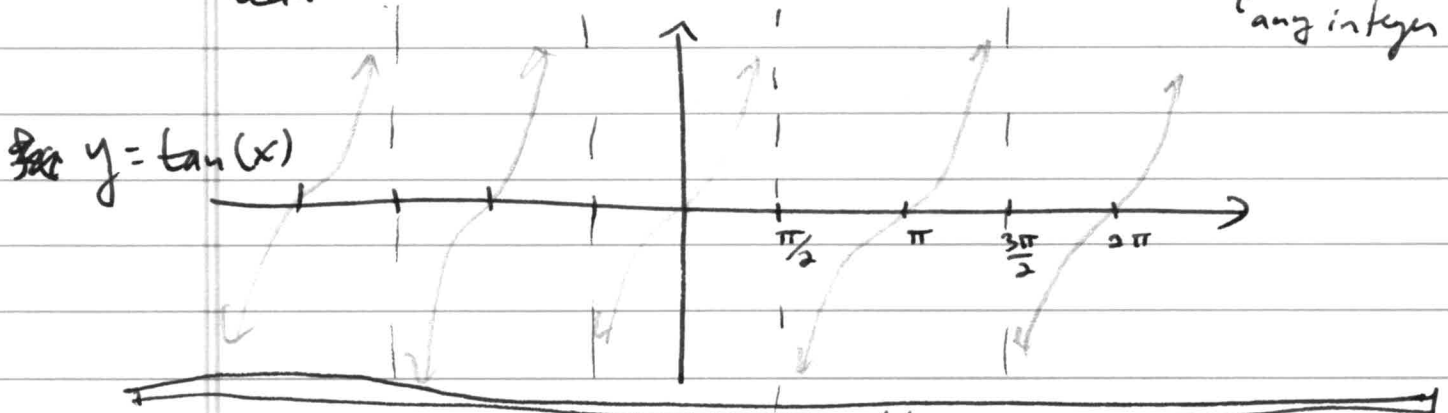


is shrunk to



to graph $f(x) = \cot(x) = \frac{1}{\tan(x)}$

~~sec~~ NOTE $f(x)$ undef'd $\Leftrightarrow \tan(x) = 0 \Leftrightarrow x = n \cdot \pi$
 \uparrow any integer



this pattern repeats
 with period π

~~sec~~ $\cot(2x)$ has period $\frac{\pi}{2}$
 $\cot(Bx)$ has period $\frac{\pi}{B}$

be able to modify graphs of \tan & \cot with \sin & \cos .

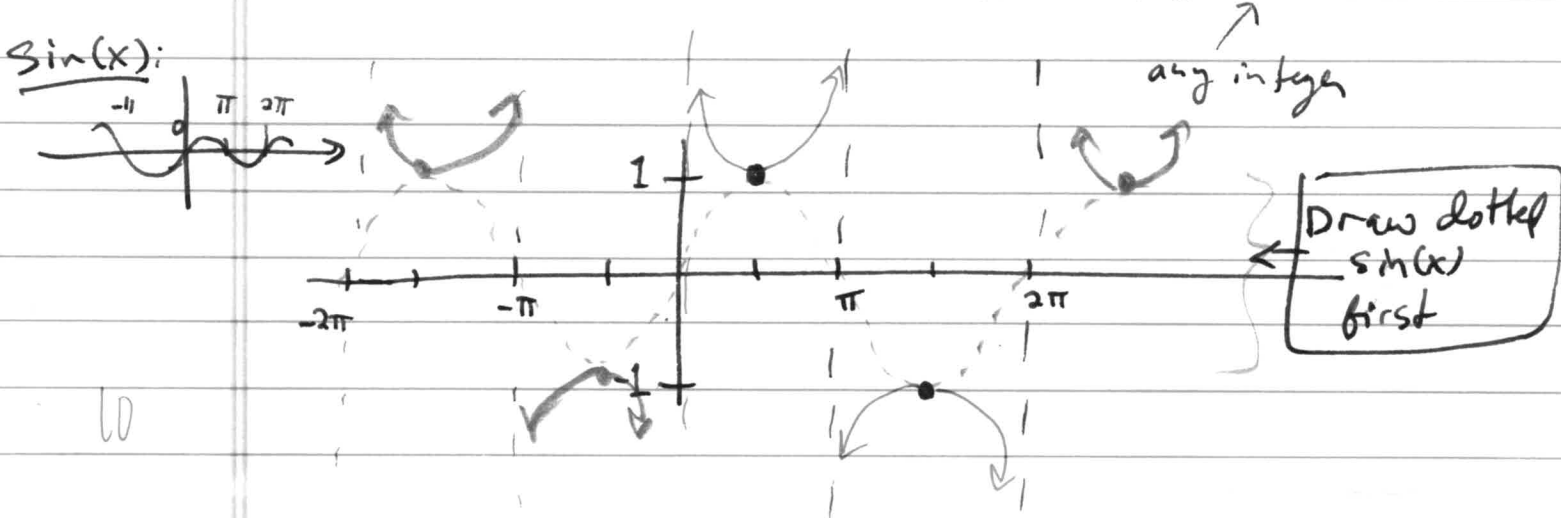
don't worry about \sec & \csc

The graphs of \csc & \sec are the widest.

$$\textcircled{B} f(x) = \csc(x) = \frac{1}{\sin(x)}$$

is undef'd $\Leftrightarrow \sin(x) = 0$

$$\Leftrightarrow x = \text{any integer} \cdot \pi$$



$$f\left(\frac{\pi}{2}\right) = \csc\left(\frac{\pi}{2}\right) = \frac{1}{\sin\left(\frac{\pi}{2}\right)} = 1$$

$$\text{as } x \rightarrow \pi, \sin(x) \rightarrow 0^+$$

$$\text{so } \frac{1}{\sin(x)} \rightarrow \infty^+$$

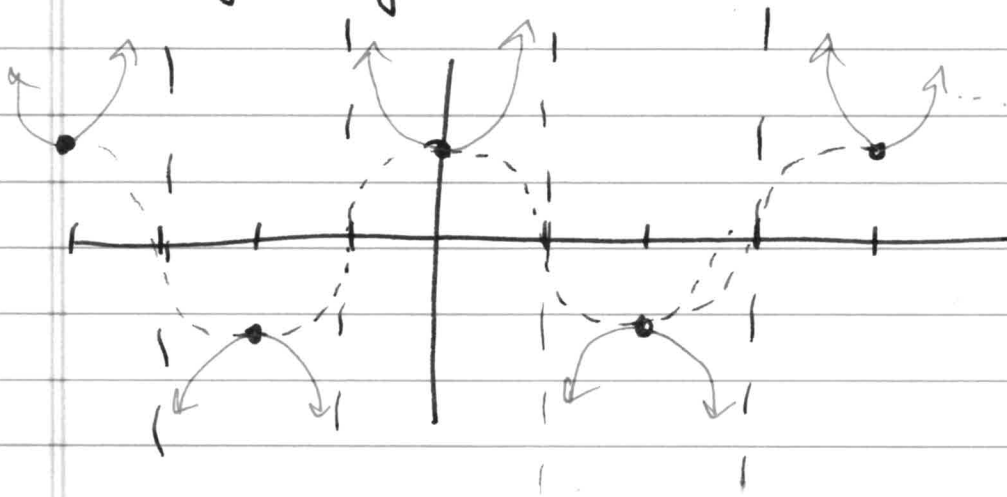
$$f\left(\frac{3\pi}{2}\right) = \csc\left(\frac{3\pi}{2}\right) = \frac{1}{\sin\left(\frac{3\pi}{2}\right)} = \frac{1}{-1} = -1$$

$$\text{as } x \rightarrow 2\pi, \sin(x) \rightarrow 0^-$$

$$\text{so } \frac{1}{\sin(x)} \rightarrow -\infty$$

& fill in rest (solid pencil)

to get $y = \sec(x) = \frac{1}{\cos(x)}$



5

to get cot, do same thing to $\tan(x)$.
(see book).